PROFESSIONAL ENGINEERS ONTARIO

National Examinations - December 2013

07-Mec-A5, Electrical & Electronics Engineering
Mechanical Engineering

3 hours duration

Name [print]:

Signature:

Notes:

[1] If doubt exists as to the interpretation of any question, the candidate is urged to submit, with the answer paper, a clear statement of any assumptions made.

[2] Candidates may use one of two calculators, the Casio or Sharp approved models. This is a closed book examination.

[3] This examination consists of the front page and 8 numbered pages.

[4] Any five (5) questions constitute a complete paper. Only the first five questions as they appear in your answer book will be marked.


[6] Clarity and organization of answers are important.

[7] The candidate is required to sign this examination paper and submit it with the solution booklets.

[8] \[ \pi = 3.14159 \]
\[ 1 \text{ hp} = 746 \text{ W} \]
\[ \mu_0 = 4\pi \times 10^{-7} \text{ H m}^{-1} \]

Front Page
QUESTION 1

Consider the transistor circuit shown in Figure 1. All transistors can be assumed to be identical with a dc current gain $\beta$.

Calculate the current transfer ratio for the circuit, $I_2 / I_1$, as a function of $\beta$.

Figure 1  Transistor Circuit
QUESTION 2

This question consists of two parts which are not necessarily related.

Part I: Design

Develop the truth table for a 2-input exclusive or gate and write the Boolean algebra expression for the output Y as a function of the inputs A,B.

You are provided with quantity six 2-input nor gates. Design the gate array to implement the 2-input exclusive or function.

Part II: Analysis

A combinational logic circuit is shown in Figure 2.

[a] Write a general Boolean algebra expression for the output C as a function of the inputs A, B, K₀, and K₁.

[b] Apply DeMorgan’s theorems and simplify the expression obtained in [a].

[c] For each of the 4 possible combinations of K₀, K₁, reduce the expression for C to its simplest form.

![Circuit Schematic](image-url)

Figure 2  Circuit Schematic
QUESTION 3

A novel type of DC machine is designed using a disc type rotor of effective outer and inner diameters D and d respectively, as shown in Figure 3. A current $I_2$ is fed radially through the rotor via two ring shaped carbon brushes. The rotor lies in the horizontal plane and is situated in a vertical magnetic field of uniform density, B Tesla. The rotor spins at an angular speed $\omega$ rad/s.

[a] Find the magnitude of the emf e generated between the brushes.

[b] Determine the torque that the rotor will be subjected to and find the output horsepower of the machine.

HINT: As a starting point, consider an elemental annulus of radius $r$ and radial length $dr$.

Figure 3 dc Machine
QUESTION 4

Part I

Consider the circuit shown in Figure 4a. A one volt (rms) ac voltage source, given by \( V = 1 \angle 0^\circ \) is connected to a parallel R-L network. The resistor R has a value of 1Ω; the impedance of the inductor is \( j1Ω \).

Calculate: [a] the current through R, \( I_1 \); [b] the current through L, \( I_2 \); [c] the total current into the network, \( I_T \); [d] the real power delivered to the load; [e] the system power factor. Note: The currents for parts [a] - [c] should be expressed as phasor quantities, of the form: \( I \angle \phi^\circ \).

![Figure 4a Circuit for Part I](image)

Part II

A capacitor is added in parallel to the inductor as shown in Figure 4b. The impedance of the capacitor is \(-j1Ω\).

Calculate: [a] the current through R, \( I_1 \); [b] the current through L, \( I_2 \); [c] the current through C, \( I_3 \); [d] the total current into the network, \( I_T \); [e] the real power delivered to the load; [f] the system power factor. Note: The currents for parts [a] - [d] should be expressed as phasor quantities, of the form: \( I \angle \phi^\circ \).

![Figure 4b Circuit for Part II](image)
QUESTION 5

Consider the circuit shown in Figure 5. Assume an ideal operational amplifier with infinite bandwidth and infinite open loop gain.

[a] Use the straight line approximation technique to sketch a plot of the magnitude of \(V_o/V_i\) in dB versus \(\log_{10}\) of frequency for a frequency range of 0.001 Hz to 10 MHz. Clearly indicate all gain levels, corner frequencies and unity gain points. Show calculations of the data used to plot your graph.

[b] A signal generator is connected to the input of the circuit.

[1] A sine wave of frequency 0.01 Hz is selected for input to the circuit.
   What is the function of the circuit at this frequency?
   Write an expression for the transfer function of the circuit in the time domain.

[2] A sine wave of frequency 1000 Hz is selected for input to the circuit.
   What is the function of the circuit at this frequency?
   Write an expression for the transfer function of the circuit in the time domain.

[3] A sine wave of frequency 1 MHz is selected for input to the circuit.
   What is the function of the circuit at this frequency?
   Write an expression for the transfer function of the circuit in the time domain.

---

**Figure 5  Circuit Schematic**

<table>
<thead>
<tr>
<th>Resistors</th>
<th>Capacitors</th>
</tr>
</thead>
<tbody>
<tr>
<td>(R_1)</td>
<td>(C_1)</td>
</tr>
<tr>
<td>160 kohm</td>
<td>1.0 (\mu)F</td>
</tr>
<tr>
<td>(R_2)</td>
<td>(C_2)</td>
</tr>
<tr>
<td>16 Mohm</td>
<td>1 pF</td>
</tr>
</tbody>
</table>

---

Component List
QUESTION 6

Part I

A dc test is performed on a 208-V, six-pole, delta connected, 60Hz induction motor, as shown in Figure 6.

[a] If $V_{DC} = 3.32$ V and $I_{DC} = 3.1$ A, calculate the per phase stator resistance, $r_1$.

Three phase excitation is applied to the motor which runs with a slip of 3.5%. Find:

[b] The speed of the magnetic field in revolutions per minute.

[c] The speed of the rotor in revolutions per minute.

[d] The electrical frequency of the rotor current.

The load on the motor is now doubled. Calculate:

[e] The speed of the rotor in revolutions per minute.

Part II

You are provided with a graph of the speed-torque characteristic of a three phase wound rotor induction motor. The torque required to drive a pump is $T = K_p n^2$ ( $K_p$ is a constant; $n$ is speed in revolutions/second). The induction motor is to be used to drive the pump. Show how you would determine the operating point speed of the system.
QUESTION 7

Consider the RC circuit shown in Figure 7. The switch $S_1$ is closed at time $t=0$, connecting the dc supply, $V_1$, to the network.

[a] Derive an expression for the voltage drop across the capacitor $C_1$ as a function of time.
[b] Derive an expression for the current delivered to the capacitor $C_1$ as a function of time.

![Figure 7 RC Circuit](image)

<table>
<thead>
<tr>
<th>COMPONENT LIST</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_1 = 30 , \text{k}\Omega$</td>
</tr>
</tbody>
</table>
QUESTION 8

Consider the magnetic circuit shown in Figure 8. An ac voltage source \( v_1(t) \) is applied to the primary winding, with \( N_1 \) turns, which results in a primary current \( i_1(t) \). A voltmeter is used to measure the voltage induced in the secondary winding \( v_2(t) \). The magnetic circuit has a mean length of \( L \) m, a cross sectional area of \( A \) m\(^2\) and a relative permeability of \( \mu_r \). The primary current is given by:

\[
i_1(t) = I_p \sin \omega t
\]

where \( I_p \) is the peak value of the primary current and \( \omega \) is the radian frequency of the supply voltage source. Neglect the resistance of the windings, leakage inductances and other losses.

[a] Develop expressions for the primary voltage \( v_1(t) \) and the secondary voltage \( v_2(t) \) as a function of the current \( i_1(t) \).

[b] Develop an expression for the impedance of this circuit as viewed from the primary.

[c] Sketch waveforms for the primary voltage \( v_{AB} \) and the secondary voltage \( v_{XY} \) showing the magnitudes and phase relations with respect to the primary current \( i_1(t) \).

![Magnetic Circuit Diagram]

**Figure 8 Magnetic Circuit**